

Henri Picciotto

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## NOTES TO THE TEACHER

Pentominoes are the geometric shapes that are formed by joining five squares edge-to-edge. The name comes from the word domino, the shape made by joining two squares in this way. There are twelve pentominoes, named after letters of the alphabet. (See the drawing at the bottom of this page.) They can be put together to form many interesting shapes.

The first known pentomino puzzle was published in 1906, but the shapes were rediscovered and named by Solomon W. Golomb at Harvard in 1953. They were popularized by Martin Gardner's "Mathematical Games" column in Scientific American.

The best-known pentomino puzzle is to cover a 6 -by-10 rectangle with all the pentominoes. Most people have trouble finding even one solution, but a computer found 2,339 of ther - $\quad$ en of this problem constitute the last two puzzles in this book.

## HOW TO USE THIS BOOK

The puzzles in this book are self-explanatory: Cover each figure with pentominoes. The pieces should not overlap or stick out beyond the boundaries of the figures.

The puzzles fall into seven sets somewhat arbitrarily titled Volcanoes, Turnarounds, Buildings, Fish, Broken Rectangles, Farms and Cracked Rectangles. As much as possible, the puzzles are ordered by difficulty within each set, the easier ones coming first. To some extent, the sets are also ordered by difficulty. You may want to keep copies of the puzzles from each set in separate folders. This will help keep the puzzles organized, and will make it easy for a student to take a whole set to his or her desk.

The names for the seven sets of puzzles were chosen, in most cases, for obvious reasons. The Volcanoes and Buildings look relatively like those objects. Turnarounds, when turned upside down (rotated 180 degrees), will still look the same. When the Fish puzzles are held diagonally some people see fish swimming in an aquarium. Broken Rectangles are all incomplete in one corner. A Farm is a rectangle with one or more rectangular holes in it. A rectangle is "cracked" if it includes a two- or three-pentomino staircase in a corner.

Some of the individual puzzles within each set have names of their own. These shapes look very much like what they are called. Perhaps these names will give your students ideas about naming some of the puzzles themselves. Encourage students to think up new titles for puzzles and to give names to some of the others.


Students may solve the puzzles in any order, but it is important they keep track of their progress by checking the puzzles on the checklist (page v) as they solve them. This allows students to see their progress and motivates them to solve more and more puzzles. If they are frustrated at a given level, encourage students to try easier puzzles. (Almost all the sets start with relatively easy puzzles.)

Use pages 1 and 2 as patterns to make pentominoes or as a check to make sure you have a complete set. If you want your students to explore pentominoes further, the following materials are available from Creative Publications.
THE MATH MACHINE-PENTOMINO PUZZLES, Cat. No. 34454 48 basic pentomino puzzles

PENTOMINO ACTIVITIES, Cat. No. 34471
Each of the 84 puzzles consists of two or more figures that must be covered simultaneously with pentominoes.

POLYOMINO LESSONS, Cat. No. 10775
PENTOMINO LESSONS, Cat. No. 34481
These pentomino and grid-paper activities help teach or reinforce many math concepts including area, perimeter, tiling, multiples, triangular numbers, congruence, similarity, maximum-minimum problems, symmetry, strategy games, problem solving, and open-ended research. These books also include dozens of very difficult puzzles.

## A NOTE ON SYMMETRY

The figures in this book can be classified into several categories from the point of view of their properties of symmetry.
Group 1
Not symmetric (most Broken Rectangles, all Cracked Rectangles).
Group 2
One line of symmetry in the direction of the pentomino boundaries (all Buildings).

## Group 3

One line of symmetry at a 45-degree angle to the pentomino boundaries (all Volcanoes, most Fish, some Broken Rectangles).

## Group 4

180-degree rotational symmetry (most Turnarounds).

## Group 5

Two perpendicular lines of symmetry in the direction of the pentomino boundaries and 180-degree rotational symmetry (some Turnarounds, most Farms).

## Group 6

Two perpendicular lines of symmetry at 45 degrees to the direction of the pentomino boundaries and 180-degree rotational symmetry (Turnaround 18, Fish 41).
Group 7
Four lines of symmetry and 90-degree rotational symmetry (Turnaround 16, Farm 65).

NAME

## CHECKLIST FOR PENTOMINO PUZZLES

Use this checklist to keep track of the puzzles you have solved.
VOLCANOES
$\begin{array}{lllllllll}3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11\end{array}$
TURNAROUNDS
$\begin{array}{llllllllllllllll}12 & 13 & 14 & 15 & 16 & 17 & 18 & 19 & 20 & 21 & 22 & 23 & 24 & 25 & 26 & 27\end{array}$
BUILDINGS
$\begin{array}{lllllllllll}28 & 29 & 30 & 31 & 32 & 33 & 34 & 35 & 36 & 37 & 38\end{array}$
FISH
$\begin{array}{lllllllll}39 & 40 & 41 & 42 & 43 & 44 & 45 & 46 & 47\end{array}$
BROKEN RECTANGLES
$\begin{array}{lllllllllllll}48 & 49 & 50 & 51 & 52 & 53 & 54 & 55 & 56 & 57 & 58 & 59 & 60\end{array}$
FARMS
$\begin{array}{lllllllllllll}61 & 62 & 63 & 64 & 65 & 66 & 67 & 68 & 69 & 70 & 71 & 72 & 73\end{array}$
CRACKED RECTANGLES
$\begin{array}{llllllllllll}74 & 75 & 76 & 77 & 78 & 79 & 80 & 81 & 82 & 83 & 84 & 85\end{array}$








## BUTTERFLY






















## HAT



## SKYSCRAPER

Buildings



Buildings









Fish
$\square$


Fish



Fish



Fish




## HEART








Broken Rectangles

$\square$

Broken Rectangles
$\qquad$

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$\square$



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Farms

|  |
| :---: |



Farms



(1)

Farms



Farms











## Cracked Rectangles



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## Solutions



Turnarounds



Fish


42 |  |  | $\square$ |
| :---: | :---: | :---: |
|  |  | $\square$ |
|  |  |  |
|  |  |  |



Broken Rectangles



60


Farms



