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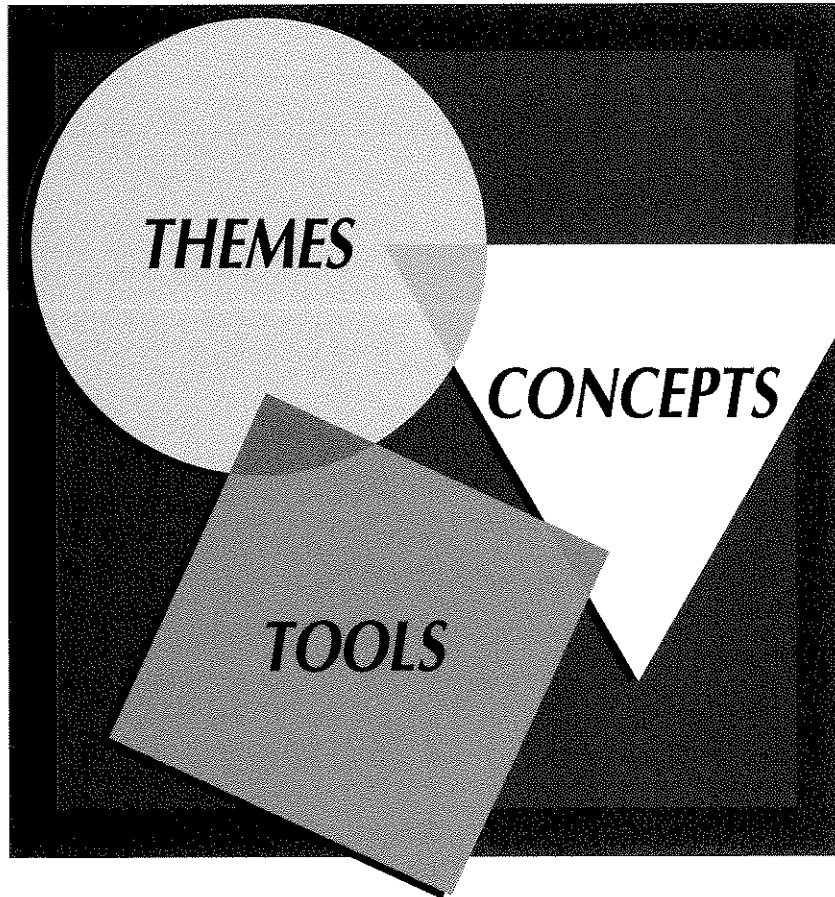


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 Creative Publications

ALGEBRA



Anita Wah
Henri Picciotto

CHAPTER

1



The spiral shape of a ram's horn

Coming in this chapter:

Exploration If you draw a closed shape by following the lines on graph paper, you can find its area and perimeter by counting. For a given area, what perimeters are possible?